

Evaluation of CO₂ Injection in Shale Gas Reservoirs Based on Numerical Simulation

Steve Wilfried Nzuetom Mbami

China University of Petroleum (East China), China

ABSTRACT

Shale gas is natural gas that is found trapped within a typical sedimentary rock derived from clastic sources which is known as shale. The combination of two advanced technologies (horizontal drilling and hydraulic fracturing) has helped to access to a large volumes of shale gas that was previously not producible. In this paper, the performance of CO₂ injection and CH₄ recovery in shale gas reservoirs is evaluated. The study reveals that it is a complex function a several parameters such as CO₂ injection time, soaking time, injection volume, reservoir permeability, reservoir porosity, and thickness. Numerical simulation is performed to model CO₂ huff-n-puff process and multicomponent Langmuir isotherms in the Barnett Shale formation; two horizontal wells are performed for this case. Results show that CO₂-EGR is very efficient for shale gas and a recovery factor of 82.6% can be obtained by this process. Besides, an analytical study is done in order to facilitate the estimation of recovery factor based on critical parameters obtained from simulation. A comparison study of the observed data from simulation and the estimated date from some production decline models such as LGA (Logistic Growth Analysis) model, and Ali model is also performed in this study.

*Corresponding author

Steve Wilfried Nzuetom Mbami, China University of Petroleum (East China), China. E-mail: nzuetomsteve@yahoo.com

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Introduction

The demand for unconventional energy, and the exploration and development of unconventional resources such as shale gas formation has gradually increased due to the rapid consumption of conventional energy [1]. Shales have these particularities that they are characterized by an extremely small grain size, low permeability and porosity, and high total organic carbon (TOC). According to Kang et al., the organic matter is a material with ultra-low porosity that consists of micropores and mesopores [2]. Natural gas in shale formation can be stored as free gas in mineral pore and organic matter [3]. Two forms for natural gas flow through shale matrix to fractures usually happen depending on the matrix being organic or inorganic. In organic matrix pores, the dominance is materialized by the transition diffusion mechanism and the effect produced by slip; however, gas-water two-phase flow controls the gas transport in inorganic matrix pores [4]. Under isothermal conditions in shale gas reservoirs (the development process is considered to be an isothermal process), there are several mechanisms for gas mass transport: viscous flow, Knudsen diffusion, adsorption/desorption effects, surface diffusion [5]. Bird et al. has discovered that the different transport mechanisms of gas in shale gas reservoirs interacted with each other, making the gas migration mode more complicated. At the same time, the special gas storage structure of reservoirs has increased the difficulty of numerical simulation rock gas reservoirs. CO₂ has been chosen here as the ideal solvent in order to enhance the gas recovery. It has been proved that shale gas has a stronger affinity to CO₂

than CH₄ (Kang SM et al., 2011; Ambrose RJ et al., 2012) which means the gas shale will absorb more CO₂ when they exist at the same time [2,6,7]. Shale and CO₂ affinity is partly of steric and thermodynamic effects, which is same with the consideration of coal for enhanced coalbed methane (ECBM) recovery [2]. One of the important mechanism of CO₂ injection is that the adsorption capacity of shale for CO₂ is larger than that for methane and some studies show that CO₂ is preferentially adsorbed over CH₄ with a ratio up to 5:1. Thus, CO₂ could replace the absorbed methane via competitive adsorption when CO₂ is introduced in shale [1,8-10].

Fathi and Akkutlu have concluded that enhanced methane recovery is divided into three stages [11]: (1) consecutive/dispersive flow gas phase (injected CO₂ released CH₄ molecules), particularly in fractures; (2) diffusive/dispersive gas transport in the secondary pore shale matrix, ie., fractures and macro-pores; and (3) multi-component sorption phenomena, particularly in primary (micro) pore structure of the shale matrix, eg., co- and counter diffusion and competitive adsorption. The effect of hydraulic fractures illustrated by Kalantari D and multi-component transport and stress change during CO₂ injection have also been conducted [12,13]. In the recent years, two special types of production modes have been done among the CO₂ injection into shale gas reservoir works: CO₂ flooding and CO₂ huff-n-puff. In CO₂ flooding, one well is used injection while the other well produces all the time. In CO₂ huff-n-puff, a well goes through three stages: injection, soaking time and production [14]. Kim et al. evaluated CO₂ injection using different shale models considering multi-component adsorption and stress-dependent permeability [13]. It is observed that both CO₂ flooding and CO₂ huff-n-puff can increase the gas recovery, though CO₂

huff-n-puff is not preferred compared to the flooding case. Also, more CO2 can be stored underground when us CO2 flooding. Liu et al. presented a novel methodology based on nuclear magnetic resonance (NMR) [15]. It can be used to measure the enhanced gas recovery (EGR) efficiency caused by CO2 injection. Sun et al. have proved that CO2 sequestration with enhanced natural gas recovery can achieve CO2 sequestration and CH4 recovery in shale gas reservoirs, and the injection pressure has a huge impact on CO2 storage and natural gas production rate [16].

Many studies have proved that the Barnett shale formation has a high potentiality of natural gas; it has been a source of interest for many researchers. Barnett shale is located in the Fort Worth Basin of northern Texas, and its potential natural gas production was discovered in 1981 by Mitchell Energy [17]. Vermynen after performing N2, CO2 and CH4 adsorption isotherms test on four Barnett shale samples, has found that and found that CH4 and N2 showed Langmuir adsorption type, while three samples demonstrated Brunauer-Emmett-Teller (BET) adsorption type for CO2 and one sample demonstrated Langmuir adsorption type for CO2. In this work, Barnett shale data is used for history matching [18]. Based on that data, we created a numerical simulation model. CMG-GEM is used here as the appropriate simulator in other to reach our goals. CO2 huff-n-puff injection in two horizontal wells is performed for sensitivity studies. Four uncertain parameters (CO2 injection time, soaking time, reservoir permeability and reservoir porosity) are revealed.

Mathematical Model for CO2 Injection in Shale Gas Reservoirs

Some assumptions are made when establishing our model: gas is stored in natural and primary fractures as free gas; in the matrix it is stored as both free and adsorbed phase. The general equations of various interactions between continuums are:

$$\frac{\partial}{\partial t} \{ \phi \rho_g x_i + (1 - \phi) m_i \} = \nabla \cdot (\rho_g x_i v) + q_i^w + q_i^{conn} \quad (1)$$

Introducing Darcy's law:

$$v = \frac{k}{\mu} (\nabla p - \gamma g \nabla D) \quad (2)$$

The formula of the mole of component i adsorbed in unit formation volume, (only for matrix):

$$m_i = \rho_R \rho_{gs} V_i \quad (3)$$

Where ϕ is the porosity of the matrix or fractured media; k is the apparent permeability of matrix or pressure-dependent permeability of fractures; μ is the gas viscosity; γ is the mass density of gas mixture; ρ_g is the gas molar density; x_i is the component mole fraction; ρ_R is the rock bulk density; ρ_{gs} is the gas molar density at standard condition; V_i is the adsorption isotherm function; q_i^w is the source/sink term of component i; q_i^{conn} is the flux terms of component i between continuums.

Physical Properties of CH4 and CO2

A good knowledge of thermodynamic properties of Methane (CH4) and carbon dioxide (CO2) is important to achieve our goal thus they have a great responsibility on monitoring transportation, optimizing compression and modeling mobility of gas in the reservoir conditions. Table 1 listed some key parameters of methane and carbon dioxide. Thus, it is important to notice that CO2 behaves as a supercritical fluid which has viscosity of a gas and density of a liquid at deep reservoir conditions. The higher density reveals that CO2 will migrate downward in the reservoir as

relative to CH4. The analysis of Chapela and Rowlinson equation deduces CO2 density. Similarly, CH4 density is obtained by using Jacobsen and Stewart equation [19,20]. It can be seen that CO2 is highly denser than CH4 throughout the reservoir pressure range. Chang et al. results have shown that by using their correlations, the CO2 solubility can be modeled. Similarly, Duan and Mao study reveals that CH4 solubility in aqueous phase can be modeled by their correlations. There are fewer tendencies to finger and intermix between the gases due to these properties [21-23].

Table 1: Matched values for reservoir and geomechanical properties from history matching

Properties	Values
Initial Reservoir Pressure	3800 psi
Porosity	0.06
Matrix permeability	0.0004 md
Reservoir Temperature	140 °F
Young's Modulus	3,887,500 psi
Poison's Ratio	0.2095
Natural Fracture Permeability	0.007 md

Adsorption of CO2 and CH4 in Barnett Shale

Previous studies have proved that the adsorption at the gas/solid interface is related to the enrichment of one or more components in the interfacial layer. Previous studies have proved that the adsorbed gas has a higher density than the surrounding non-adsorbed gas. According to Clarkson and Haghshenas there are five mechanisms for methane existence in shale gas reservoirs: Adsorption upon internal surface area, conventional (compressed gas) storage in natural and hydraulic (induced) fractures, conventional storage in matrix porosity (organic and inorganic), solution in formation water, and absorption (solution) in organic matter. According to the International Union of Pure and Applied Chemistry (IUPAC) standard classification system there are six different types of adsorption, as in Figure 1. The classic Langmuir isotherm (Type I) is considered as the most commonly applied monolayer adsorption model for shale gas reservoirs. It is based upon the assumption that there is a dynamic equilibrium at constant temperature and pressure between adsorbed and non-adsorbed gas [24-26]. The following formula described the Langmuir isotherm with two fitting parameters:

$$V(P) = \frac{V_L P}{P + P_L} \quad (4)$$

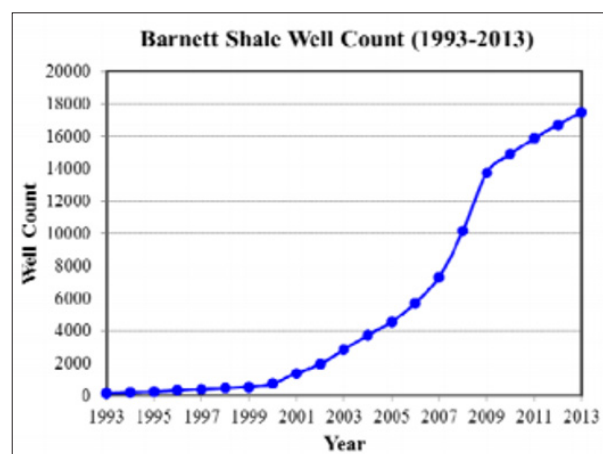


Figure 1: Barnett Shale well count. Source: Texas Railroad Commission (modified from Texas Railroad Commission, 2013)

Where $V(P)$ is the gas volume of adsorption at pressure P , V_L is Langmuir volume, referred to as the maximum gas volume of adsorption at the infinite pressure, P_L is Langmuir pressure, which is the pressure corresponding to one-half Langmuir volume. According to Gao et al. the instantaneous equilibrium is a reasonable assumption because ultra-low permeability in shale leads to very low flow rate through the kerogenic media within shale. It is also assumed to be established for the Langmuir isotherm. In the case of multilayer sorption of gas occurs, the BET isotherm (Type II) should be a better model the following equation materialize that fact [27-29]:

$$V(P) = \frac{V_m CP}{(P_o - P)[1 + (C - 1)P / P_o]} \quad (5)$$

Where P_o is the saturation pressure of the gas, V_m is the maximum adsorption gas volume when the entire adsorbent surface being covered with a complete unimolecular layer, C is a constant related to the net heat of adsorption. Figure 2 describes other isotherm types [24].

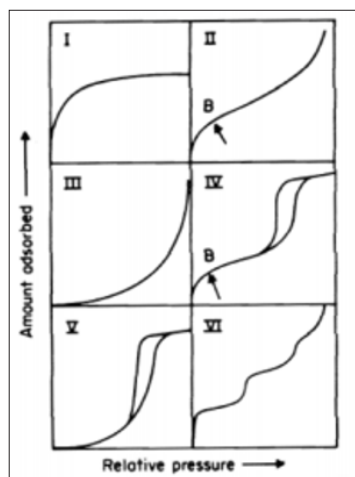


Figure 2: The six types of Physisorption isotherms according to the IUPAC classification (Sing et al., 1985).

Numerical Simulation Model

In this work, CMG-GEM simulator is used to model CO2 flow in a shale gas reservoir. Arri et al, 1992; Hall et al., 1994 through GEM simulator used an extended Langmuir isotherm for modeling multicomponent adsorption and desorption. The following formula is best explicit [30,31]:

$$w_i = \frac{w_{i_{max}} B_i y_{ig} p}{1 + p \sum_j B_j y_{jg}} \quad (6)$$

Where w_i is the moles of adsorbed component i per unit mass or rock, $w_{i_{max}}$ is the maximum moles of adsorbed component i per unit or rock, B_i is the parameter for Langmuir isotherm relation, p is pressure, and y_{ig} is the molar fraction of adsorbed component i in the gas phase, i and j are component indices including CH_4 , N_2 , CO_2 , or coal. To evaluate the effects of CO2 injection in shale gas reservoir, a 3D shale reservoir model of 30 ft × 20 ft × 10 ft

Grid cells dimension in Figure 3 was built based on the properties of history matching. History matching was performing by using the field data of Barnett shale reproduced from Anderson et al. the matched values, segment of the rese, and other properties are shown in Table 1. The average matrix permeability of the reservoir is 24 mD and average porosity 0.4%. The average thickness of the reservoir is 5ft and the reservoir temperature is a constant 140 °F. Figure 4 shows the average reservoir pressure during the whole life of the reservoir [32].

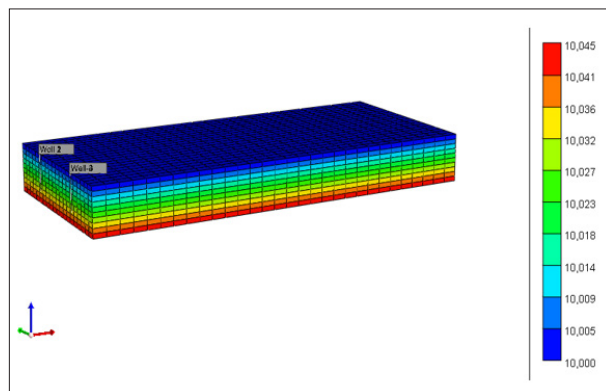


Figure 3: 3D reservoir model including 2 horizontal wells

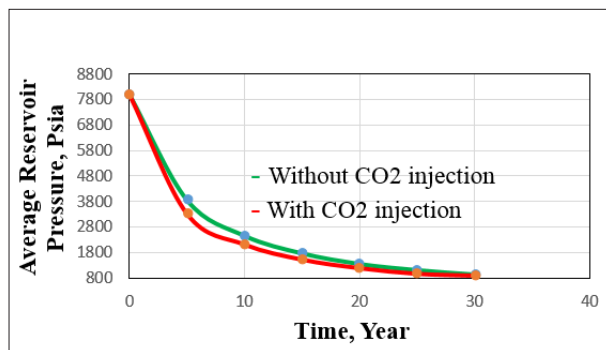


Figure 4: Average reservoir pressure with and without CO2 injection

Results and Discussion

Two horizontal wells were performed in this work. Based on our previous researches, we chose CO2 huff-n-puff process in other to minimize spending. This process is applying to the two wells at the same time. For our base case, we injected CO2 for 6 months; after that we shut-in the wells for a period of time (soaking time) of 3 months and finally wells started producing for 24 months. The cycle is repeating until the end of the production period of 30 years. Figure 5 and Figure 6 indicate respectively the gas recovery and the cumulative gas production with and without CO2 injection. We can notice that the recovery factor of the gas is lower without CO2 injection, thus it is useful for the displacement of the methane. The adsorbed moles of CH_4 and CO_2 without considering multicomponent adsorption mechanism is presented in Figure 7. The figure shows that the potential adsorption of CH_4 decreases with the production time while there is not CO_2 adsorption. Figure 8 shows the total volume of CO_2 injected in the reservoir. It can be seen that a total amount of 350 Mscf of CO_2 is injected.

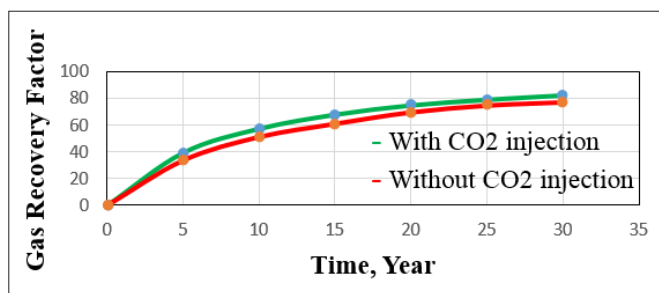


Figure 5: Comparison of gas recovery factor with and without CO2 injection

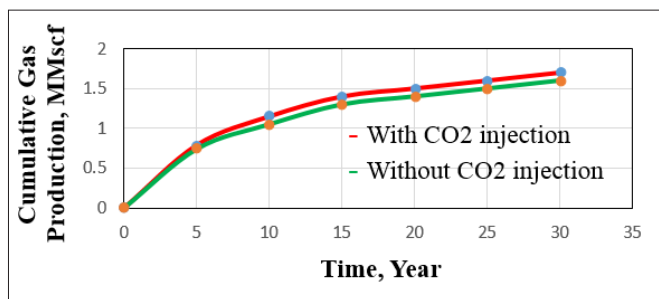


Figure 6: Cumulative gas production with and without CO2 injection

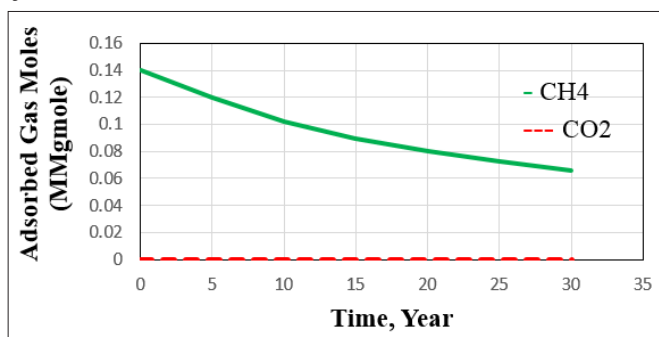


Figure 7: Adsorbed gas moles for CO2 and CH4 without considering multi-component adsorption

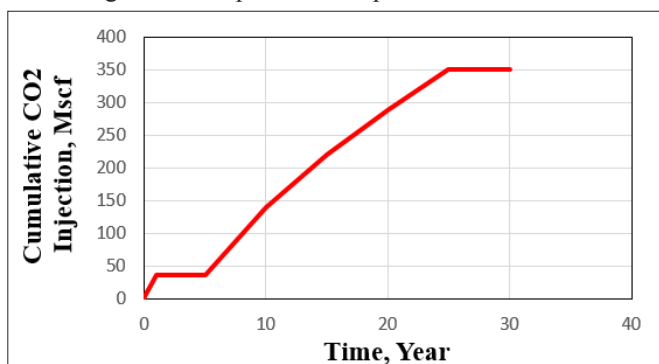


Figure 8: Total volume of CO2 injected

A sensitivity study was done in order to analyze all the parameters that can affect the methane recovery. Due to many estimable and uncertain parameters such as reservoir permeability, porosity, fracture half-length, and fracture conductivity there is a high uncertainty in shale gas reservoirs 33-35. The present work considered four uncertain parameters such as reservoir permeability, porosity, CO2 injection time, and number of cycle (as listed in Table 2) for maximizing the methane recovery. Figure 9 shows that the increase of the reservoir permeability increases

the methane recovery. This is because the increase of permeability affects directly the mobility ratio then affects the gas recovery. The maximum value of gas recovery factor obtained is 89.4 %. The effect of the reservoir porosity on the methane recovery is shown in Figure 10. We can understand that the increase of reservoir porosity increases the gas recovery. The maximum value of gas recovery obtained is 86.4%. Figure 11 and Figure 12 respectively analyze the effect of CO2 injection time and the number of cycle on gas recovery. It can be seen that they increase the methane recovery in a certain condition. The maximum values of gas recovery obtained are respectively 83.3% and 82.6%.

Table 2: Four uncertain parameters used for sensitivity study

Parameter	Value 2	Base Case	Value 3
Reservoir Permeability	0.0008	0.0004	0.009
Reservoir Porosity	0.03	0.06	0.09
CO2 Injection Time	3	6	9
Number of Cycle	3	11	7

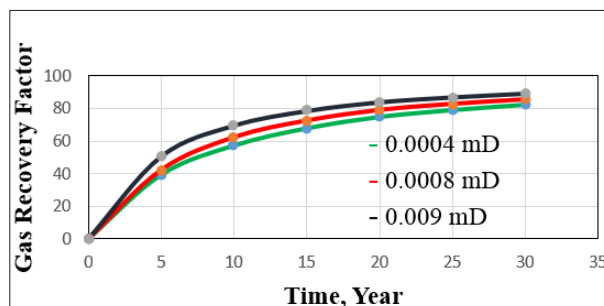


Figure 9: Effect of Reservoir permeability on gas recovery factor

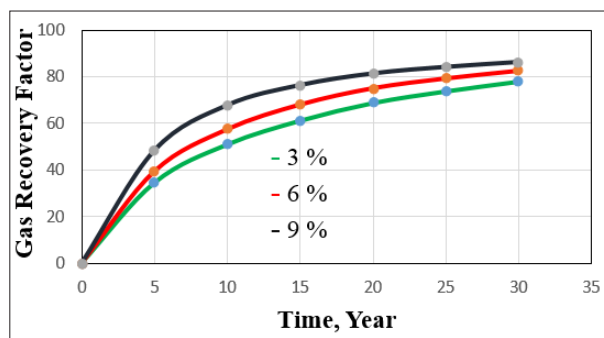


Figure 10: Effect of Reservoir porosity on gas recovery factor

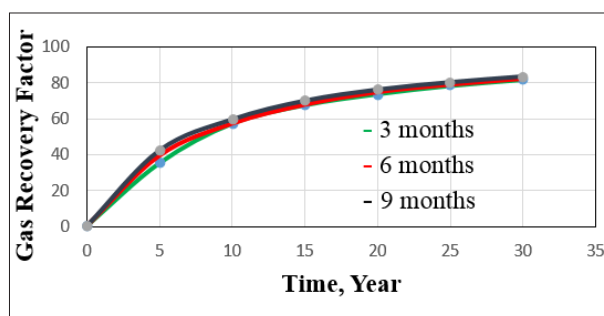


Figure 11: Effect of CO2 injection time on gas recovery factor

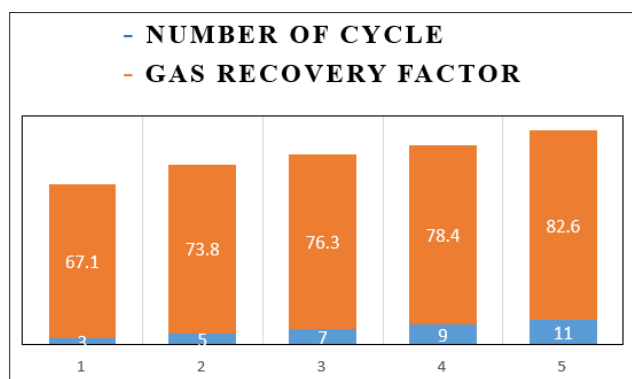


Figure 12: Effect of number of cycle on gas recovery factor

Besides, some regression equations were built for analytical solutions. These equations are obtained based on simulation results. They can be used to get an approximated value of the gas recovery factor just by replacing the unknown X by the value of one of the uncertain parameters listed above. Figure 13, Figure 14 and Figure 15 respectively illustrate the gas recovery in function of reservoir permeability, number of cycle, and CO2 injection time.

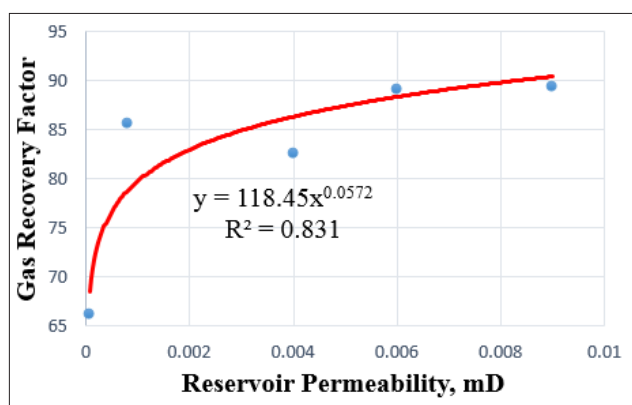


Figure 13: Gas recovery factor versus reservoir permeability

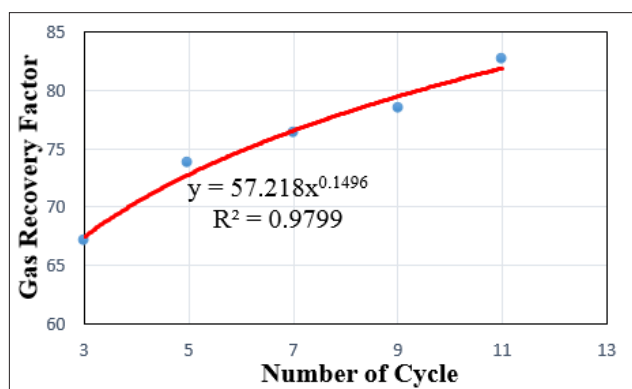


Figure 14: Gas recovery factor versus number of cycle

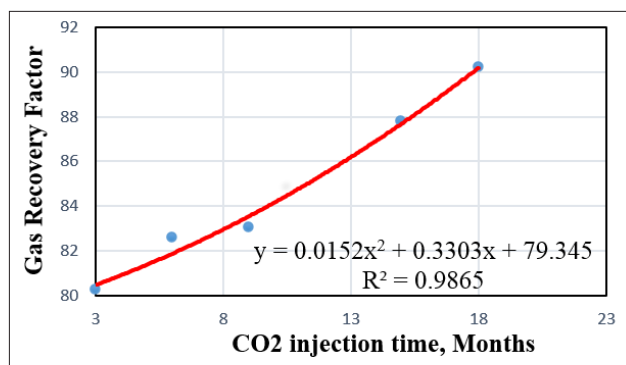


Figure 15: Gas recovery factor versus CO2 injection time

Finally, a comparison study observed data (from simulation results) and estimated data (from production decline models) was performed. Two production decline models have been chosen for our work: Logistic Growth Analysis (LGA) model and Ali model. Clark et al. by matching the logistic growth model to the production data of some wells have built an update time-rate function [36]. LGA model is proposed for estimating production forecasting of reservoirs with extremely low permeability [36,37]. The following equation has been derived from the hyperbolic group of curves and is usually used for the cumulative production estimation;

$$Q(t) = \frac{Kt^n}{a+t^n} \quad (7)$$

where K is the carrying capacity or the maximum recoverable gas from the reservoir. 'a' constant is t^n at which half of the recoverable gas has been produced. 'n' is the hyperbolic exponent.

In our study, the parameters K, a and n were estimated using Excel's multivariable solver tool. Comparison of the observed cumulative production with the one obtained by using Eq.7 has been done. The model has the same trend as the observed data but diverges from time to time as shown in Figure 16.

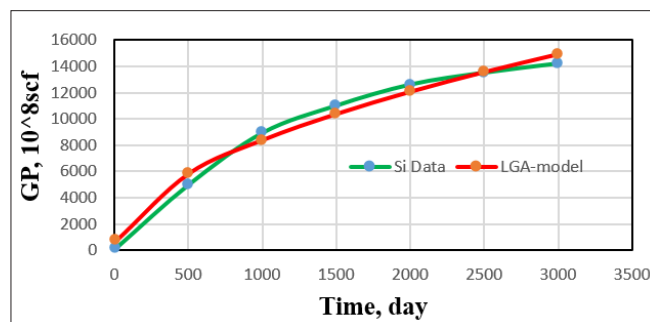


Figure 16: LGA model fit to cumulative gas production

Ali et al. have found that the plot of the cumulative gas production in function of time is a straight line with the slope equal to 1 if the flowing pressure of the production well is constant. However, many analyses have proved that the best relationship between both variables is:

$$G_p = ct^n \quad (8)$$

Where c is the intercept constant and n ($=dt^{-n}$) is the slope parameter which is a time function defined as a power law function. The first step is to fit Eq.8 into the observed cumulative gas production to

estimate constant (c) using linear regression. Figure 17 shows the corresponding best fit parameter for the intercept $c = 28.661$ 1/d. The next step is to estimate the change of slope (n) with time. The change of slope (n) can be calculated by inverting Eq.8 for each time step as $n(\text{slope}) = (\log(G_{p2}) - \log(G_{p1})) / (\log(t_2) - \log(t_1))$. Then we draw the slope points versus time on log-log plot. Figure 18 shows the change of slope over time, the best fit regression function is $n = 1.554 t^{-0.179}$. Comparison of the observed cumulative production with the one obtained by using Eq.8 has been done. The model's trend is the same with the observed data one. It matches the observed data at the beginning, then it starts diverging as shown in Figure 19.

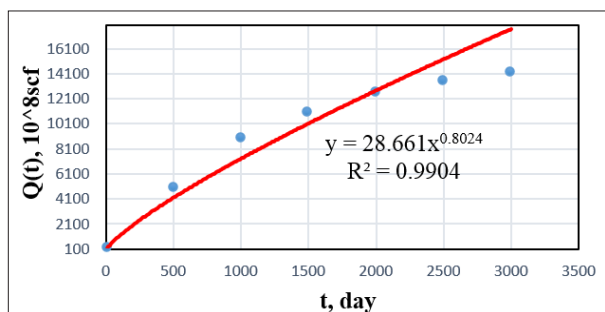


Figure 17: Cumulative gas production vs. actual time for Ali Model

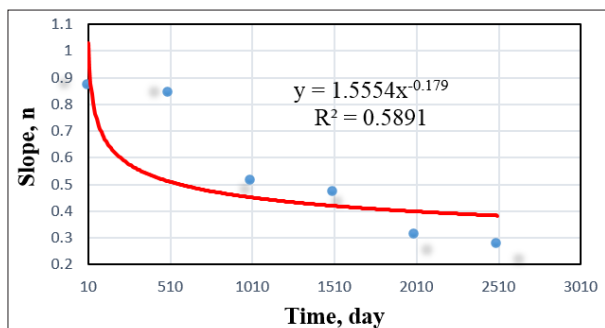


Figure 18: Slope (n) vs. actual time for Ali Model

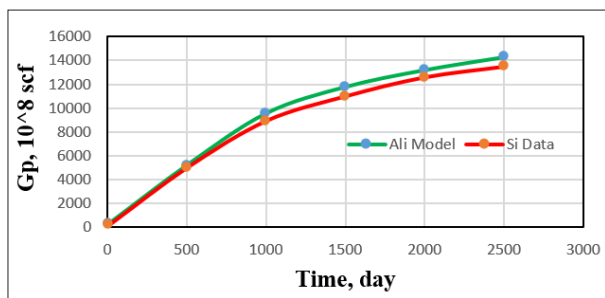


Figure 19: Ali model fit to cumulative gas production

Conclusion

In this study, a series of simulations have been done in order to evaluate the CO₂-enhanced gas recovery in shale gas reservoirs. The following conclusions have been brought out:

1. Injection CO₂ into shale gas reservoir can really enhance the gas recovery. Some parameters such as reservoir permeability, reservoir porosity, CO₂ injection time and the number of cycle have a great effect on the methane recovery.
2. A comparison of the gas recovery factor with and without CO₂ injection has illustrated that the effect is higher when CO₂ is injected.
3. The physical properties of CO₂ and CH₄ have proved that the range 3500-4700 ft is suitable for enhancing methane

recovery and CO₂ storage.

4. In the case of non-considering multicomponent adsorption there is not an adsorbed CO₂ during the whole process.
5. LGA model and Ali model are two suitable models for estimating production forecasting of an unconventional reservoir.

Nomenclature

TOC	=	Total Organic Component
EGR	=	Enhanced Gas Recovery
LGA	=	Logistic Growth Analysis
ECBM	=	Enhanced Coalbed Methane
NMR	=	Nuclear Magnetic Resonance
BET	=	Brunauer Emmett Teller
IUPAC	=	International Union of Pure and Applied Chemistry
ϕ	=	Porosity
K	=	Permeability, md
ρ_g	=	Gas molar density,
x_i	=	Component mole fraction
m_i	=	Adsorbed mole in unit formation volume, kmol.ft ⁻³
q_i^w	=	Source/sink term, kmol.ft ⁻³
q_i^{com}	=	Flux term between continuums, kmol.ft ⁻³ .d ⁻¹
u	=	Darcy velocity, ft ² .d ⁻¹
γ	=	Gas mass density, ton.ft ⁻³
ρ_{gs}	=	Gas molar density at standard condition, kmol.ft ⁻³
V_i	=	Adsorption term, ft ³ .ton ⁻¹)
V_L	=	Langmuir volume, Scf/ton
P	=	Pressure, Psi
P_L	=	Langmuir pressure, Psi
V	=	Maximum adsorption gas volume, Scf/ton
C	=	Constant relate to the net heat adsorption
P_o	=	Saturation pressure of the gas, Psi
W_{imax}	=	Maximum moles of adsorbed component i per unit mass or rock, mole
B_i	=	Parameter for Langmuir isotherm relation
y_{ig}	=	Molar fraction of adsorbed component i in the gas phase
a	=	Intercept constant defined in LGA Model
k	=	Maximum recoverable gas from the reservoir
G_p	=	Cumulative gas production, Scf
C	=	Intercept constant defined in Ali Model

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